



# Uncertainty quantification of the optical model for fission fragment de-excitation

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# Mission Relevance

**Fission produces key observables for special nuclear material detection and quantification:**

- Average neutron multiplicity  $\bar{\nu}$
- neutron multiplicity distributions,  $P(\nu)$ , and factorial moments  $E \left[ \frac{\nu!}{(\nu-m)!} \right]$ ,
- neutron energy spectra;  $\chi(E)$ ,
- correlations: neutron-photon multiplicity, energy, angle, ...

**... but it is complex and hard to model**



# Motivation: simulate event-by-event fission with uncertainty

- Tabulated evaluated data (ENDF, JENDL, JEFF, ...):
  - + **uncertainty**
  - **no event-by-event correlations**
- Model-based event generators ([CGMF](#), Freya, ...):
  - **no/limited uncertainty**
  - **computationally expensive**
  - + **event-by-event correlations**

**Goal: add uncertainty estimates to physics-based fission models**



# Physics based fission models use the optical model

**Monte Carlo Hauser Feshbach** fragment de-excitation:

- Start with post-scission fragment in some channel  $(J, \pi, E)$
- Until stable, sample decay from current channel  $a \rightarrow \{b, c, d, \dots\}$ :

$$P(a \rightarrow b) \approx \frac{T_a T_b \rho(b)}{\sum_i |T_i|^2 \rho(i)}$$

Approximate transmission coefficients  $T_a$  using **the Optical Model**



# The optical model is our best option, but it isn't perfect

- Optical model parameterizes mean-field nuclei-nucleon potential:
  - Microscopic: chiral effective field theory, ...
  - Phenomenological: scattering experiments; local (single A,Z) or global
- Common choice: Koning-Delaroche global optical model
  - 5 terms
  - 36 parameters; fit to global neutron elastic scattering data

**Fission fragments: too unstable for local phenomenological; too heavy for microscopic. How well do global models extrapolate?**



# Technical Approach to uncertainty quantification

## Dr. Cole Pruitt:

Markov-chain Monte Carlo to determine distribution of Koning-Delaroche optical model parameters conditional on scattering data

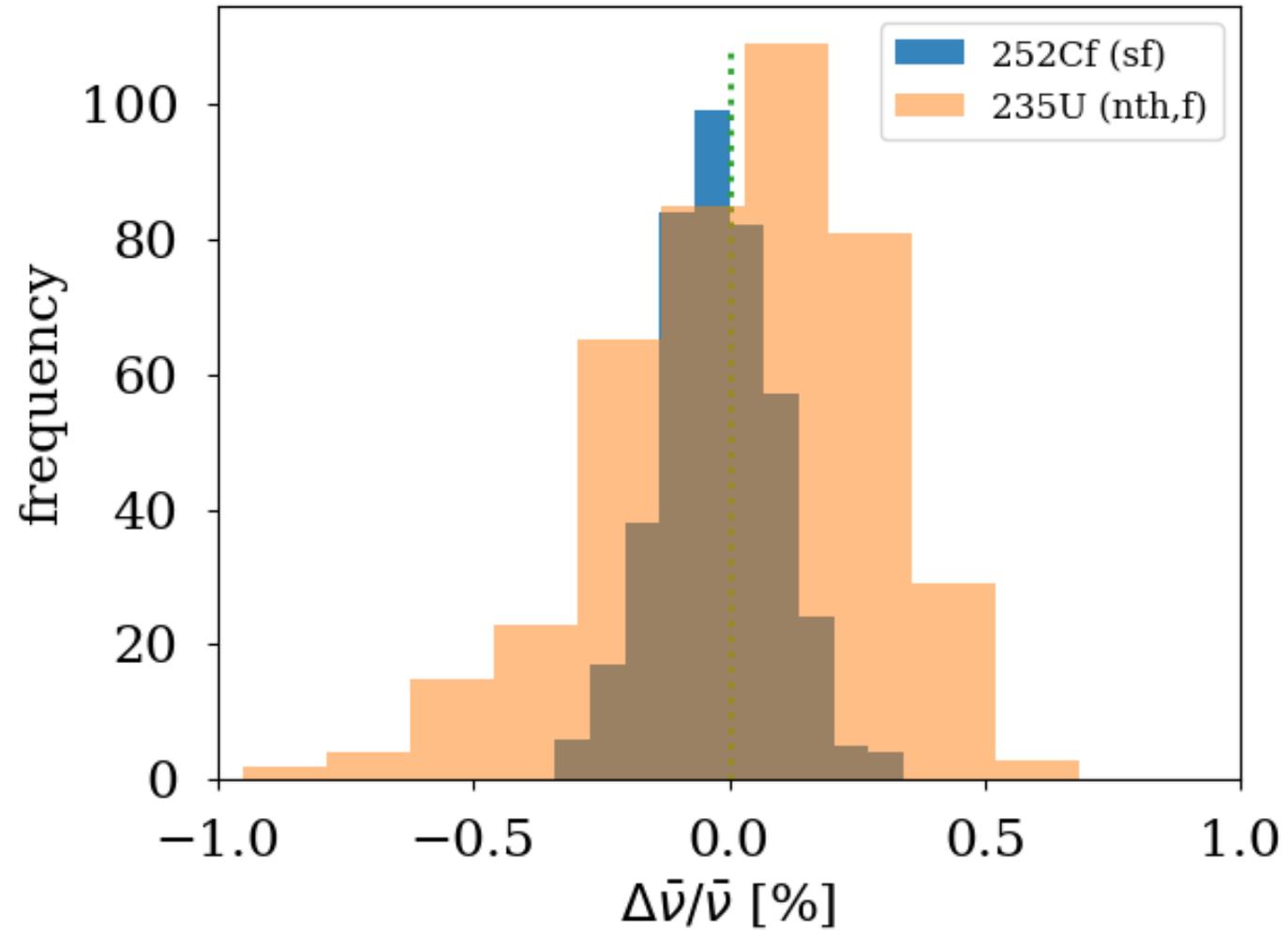


## This work:

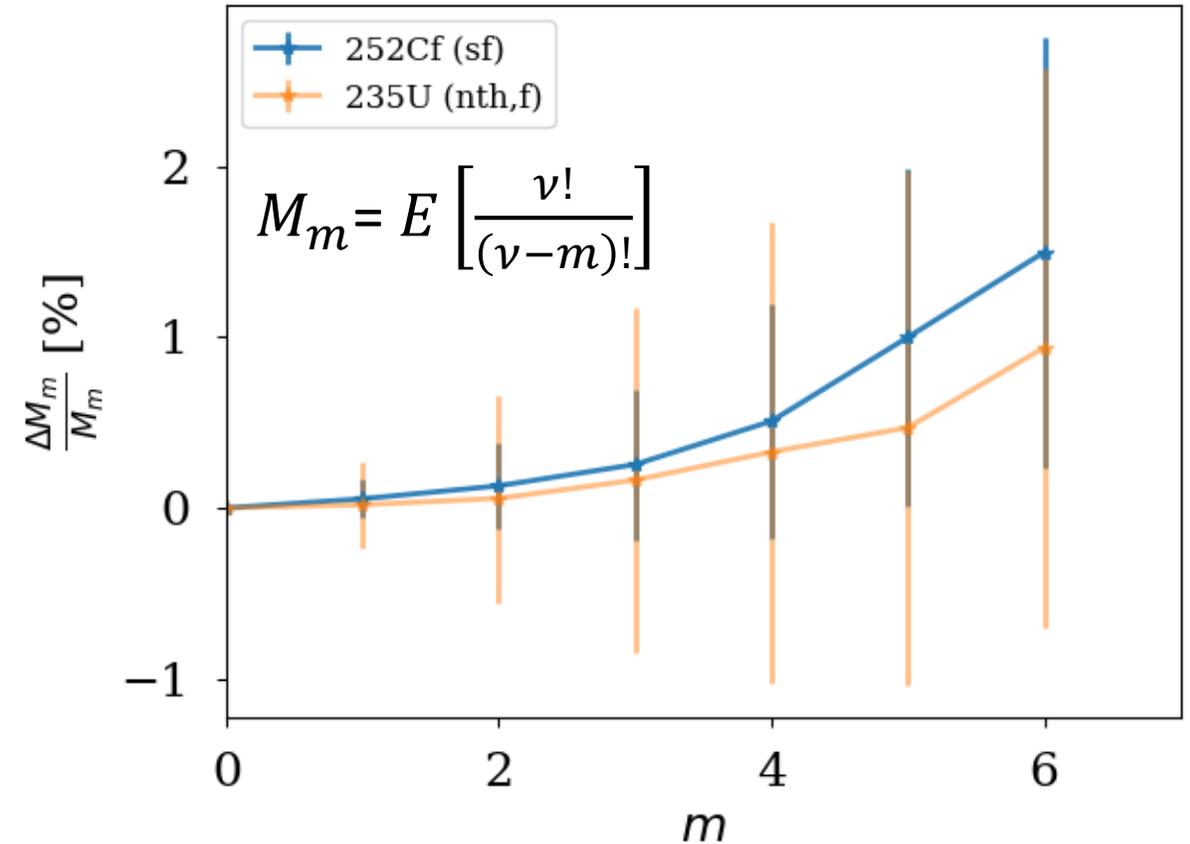
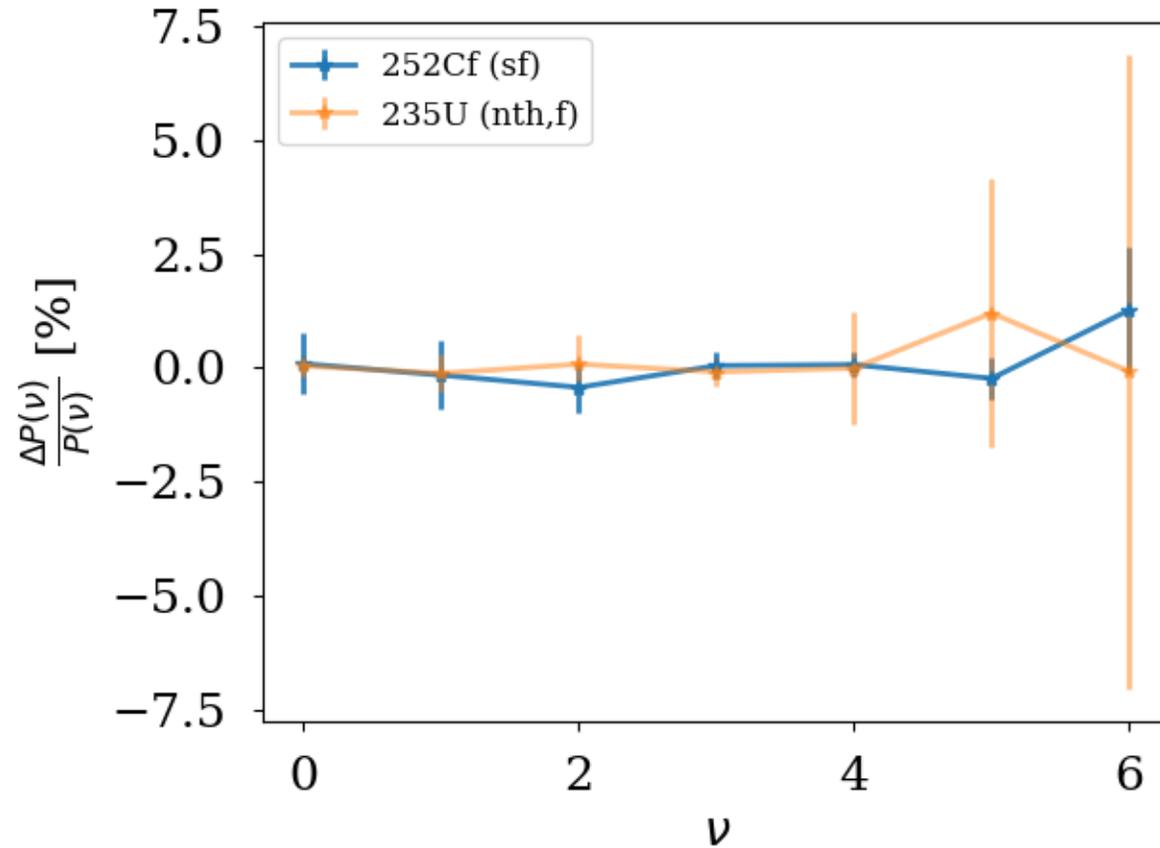
Sample from optical model parameter distributions to calculate ensemble of fission observables in CGMF



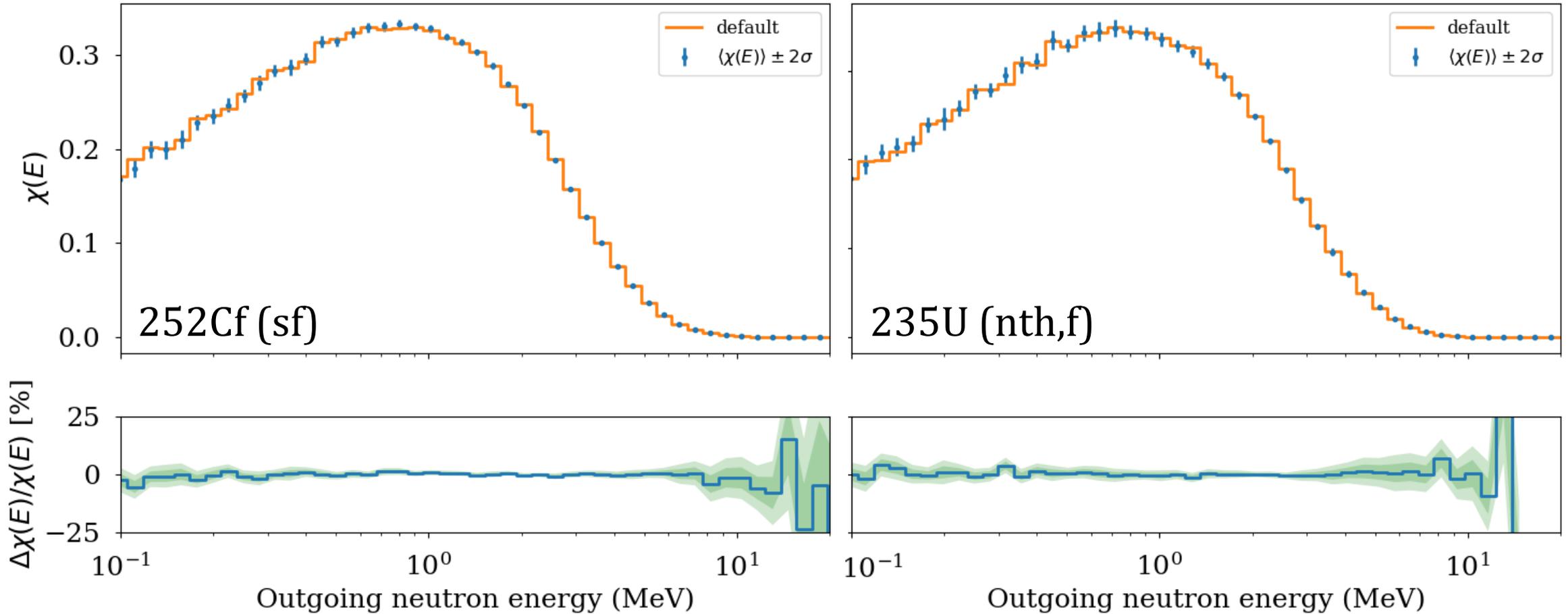
# Uncertainty in $\bar{\nu}$ : greater for $^{235}\text{U}$ (nth,f)



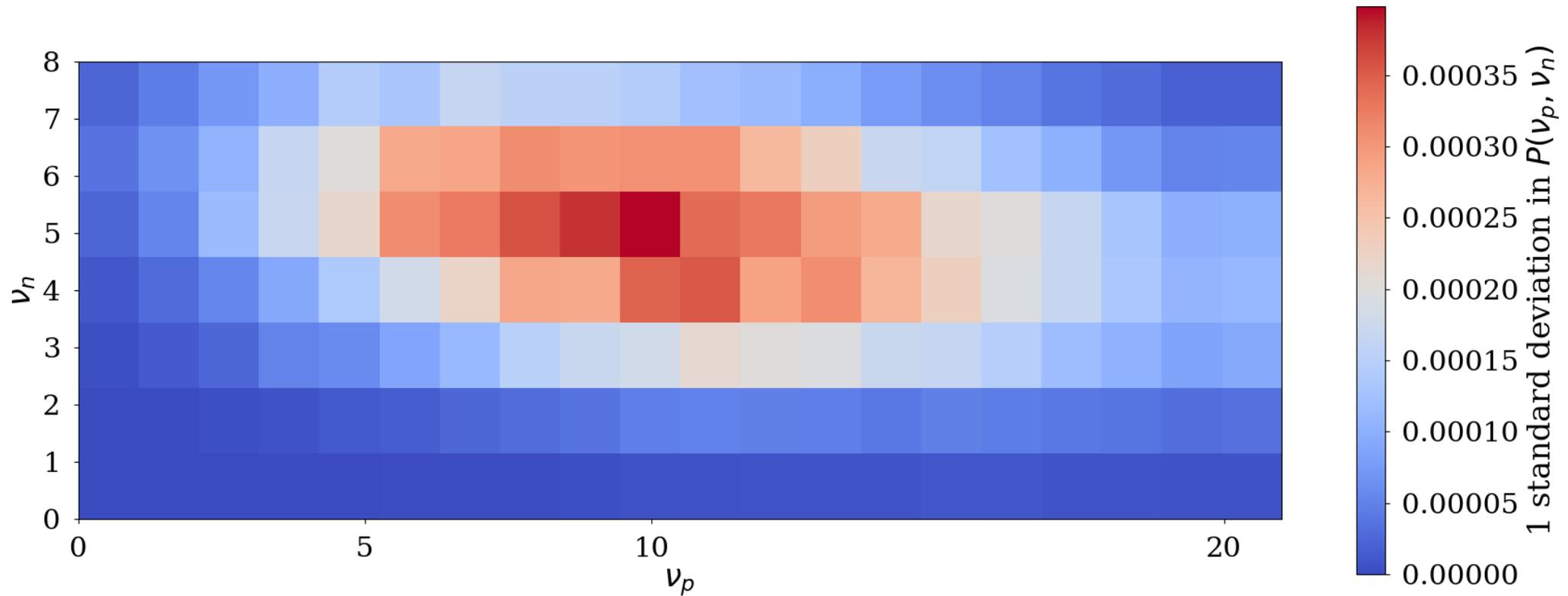
# Neutron multiplicity distributions and factorial moments



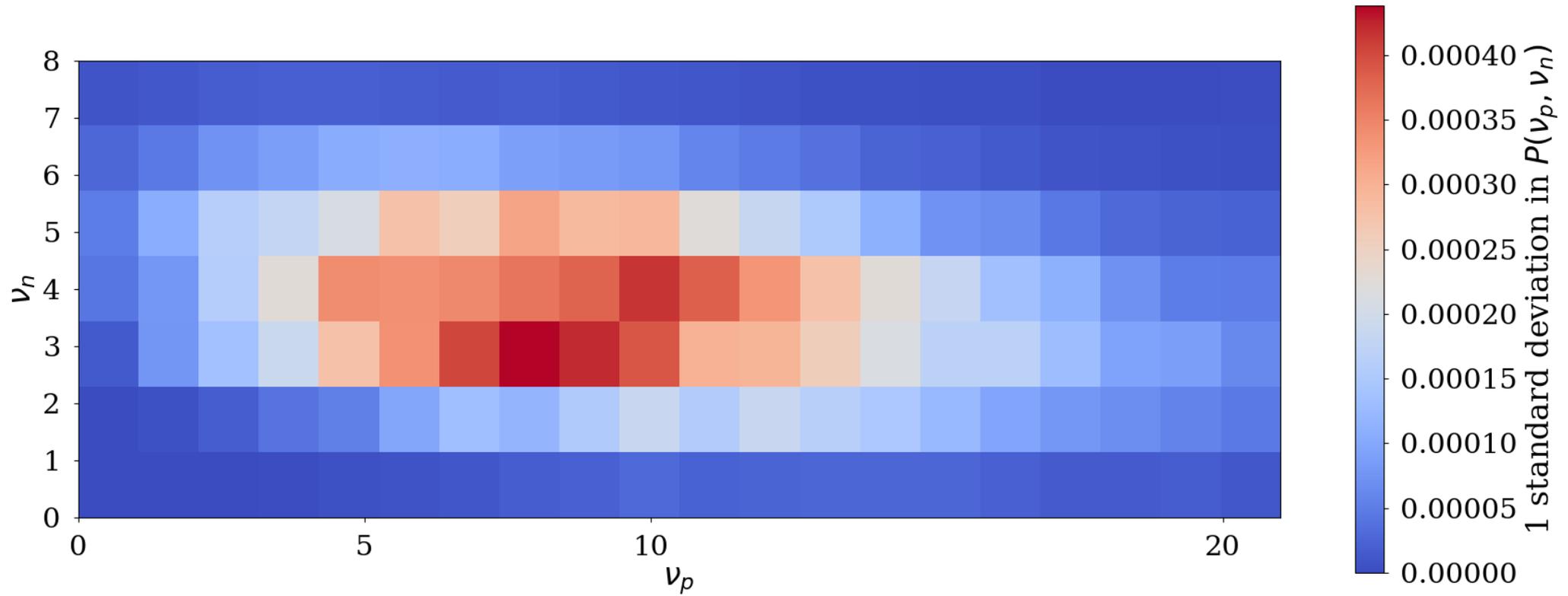
# Uncertainty in $\chi(E) \approx 5\%$ at low energy, 25% high energy



# 252Cf correlated n,p multiplicity



# U235 correlated n,p multiplicity



# Expected Impact

- **A step towards uncertainty in event-by-event fission models**
- Explore open questions in fission/fission modeling:
  - CGMF  $\chi(E)$  high-energy tail smaller than experiment
  - How do fragments remove angular momentum?

# MTV Impact

- Ongoing collaboration with Dr. Cole Pruitt at LLNL
  - Dr. Meghan McGarry connected Dr. Pruitt and I following discussion @UPR21
- Collaboration on global UQ/parameter optimization wrt fission observables with Dr. Amy Lovell at LANL



# Conclusions

- Calculated covariances in fission observables due to model parameter uncertainty in the Koning-Delaroche global optical model
- Software developed is open source:
  - Optical model neutron-nuclei scattering code: [github.com/beykyle/opxs](https://github.com/beykyle/opxs)
  - Modified version of CGMF for this work: [github.com/beykyle/CGMF](https://github.com/beykyle/CGMF)
  - UQ workflow: [github.com/beykyle/omp-uq](https://github.com/beykyle/omp-uq)

## Future work

- Explore model form uncertainty with other optical models, including microscopic (**add microscopic info -> improve extrapolation to fragments?**)
- Look at fragment specific observables, angular momentum, correlations



# References

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